# STATICS AND MECHANICS OF MATERIALS

SIXTH EDITION IN SI UNITS

# CONTENTS



#### 1 General Principles 31

Chapter Objectives 31

- 1.1 Mechanics 31
- **1.2** Fundamental Concepts 32
- **1.3** The International System of Units 36
- 1.4 Numerical Calculations 38
- **1.5** General Procedure for Analysis 40



# 2 Force Vectors 45

- 2.1 Scalars and Vectors 45
- 2.2 Vector Operations 46
- 2.3 Vector Addition of Forces 48
- 2.4 Addition of a System of Coplanar Forces 58
- 2.5 Cartesian Vectors 67
- 2.6 Addition of Cartesian Vectors 70
- 2.7 Position Vectors 77
- 2.8 Force Vector Directed Along a Line 79
- 2.9 Dot Product 86



#### **3** Force System Resultants 101

Chapter Objectives 101

- **3.1** Moment of a Force—Scalar Formulation 101
- **3.2** Principle of Moments 103
- 3.3 Cross Product 111
- **3.4** Moment of a Force—Vector Formulation 114
- **3.5** Moment of a Force about a Specified Axis 124
- 3.6 Moment of a Couple 132
- **3.7** Simplification of a Force and Couple System 142
- **3.8** Further Simplification of a Force and Couple System 152
- **3.9** Reduction of a Simple Distributed Loading 162

## **4** Equilibrium of a Rigid Body 175

- **4.1** Conditions for Rigid-Body Equilibrium 175
- 4.2 Free-Body Diagrams 177
- 4.3 Equations of Equilibrium 186
- 4.4 Two- and Three-Force Members 192
- 4.5 Free-Body Diagrams 201
- 4.6 Equations of Equilibrium 206
- 4.7 Characteristics of Dry Friction 214
- 4.8 Problems Involving Dry Friction 219





# Structural Analysis 237

5

Chapter Objectives 237

- 5.1 Simple Trusses 237
- 5.2 The Method of Joints 240
- 5.3 Zero-Force Members 246
- The Method of Sections 252 5.4
- 5.5 Frames and Machines 261



#### 6 Center of Gravity, Centroid, and Moment of Inertia 285

- Center of Gravity and the Centroid of a 6.1 Body 285
- 6.2 Composite Bodies 298
- 6.3 Moments of Inertia for Areas 306
- 6.4 Parallel-Axis Theorem for an Area 307
- Moments of Inertia for Composite 6.5 Areas 314



#### 7 Stress and Strain 325

Chapter Objectives 325

- 7.1 Introduction 325
- 7.2 Internal Resultant Loadings 326
- 7.3 Stress 338
- 7.4 Average Normal Stress in an Axially Loaded Bar 340
- 7.5 Average Shear Stress 347
- 7.6 Allowable Stress Design 358
- 7.7 Deformation 373
- 7.8 Strain 374



# 8

# Mechanical Properties of Materials 391

- 8.1 The Tension and Compression Test 391
- 8.2 The Stress–Strain Diagram 393
- **8.3** Stress-Strain Behavior of Ductile and Brittle Materials 397
- 8.4 Strain Energy 401
- 8.5 Poisson's Ratio 410
- 8.6 The Shear Stress–Strain Diagram 412



# 9 Axial Load 423

Chapter Objectives 423

- 9.1 Saint-Venant's Principle 423
- **9.2** Elastic Displacement of an Axially Loaded Member 425
- 9.3 Principle of Superposition 438
- **9.4** Statically Indeterminate Axially Loaded Members 438
- **9.5** The Force Method of Analysis for Axially Loaded Members 445
- 9.6 Thermal Stress 451
- 9.7 Stress Concentrations 458



# 10 Torsion 467

- **10.1** Torsional Deformation of a Circular Shaft 467
- 10.2 The Torsion Formula 470
- 10.3 Power Transmission 478
- 10.4 Angle of Twist 488
- **10.5** Statically Indeterminate Torque-Loaded Members 502
- \*10.6 Solid Noncircular Shafts 509
- 10.7 Stress Concentration 512





# 11 Bending 523

Chapter Objectives 523

- **11.1** Internal Loading as a Function of Position 523
- **11.2** Graphical Method for Constructing Shear and Moment Diagrams 530
- **11.3** Bending Deformation of a Straight Member 547
- **11.4** The Flexure Formula 551
- 11.5 Unsymmetric Bending 564
- **11.6** Stress Concentrations 572

# 12 Transverse Shear 581

- 12.1 Shear in Straight Members 581
- 12.2 The Shear Formula 582
- **12.3** Shear Flow in Built-Up Members 598





# 13 Combined Loadings 611

Chapter Objectives 611

- 13.1 Thin-Walled Pressure Vessels 611
- **13.2** State of Stress Caused by Combined Loadings 618

## 14 Stress and Strain Transformation 639

- 14.1 Plane-Stress Transformation 639
- **14.2** General Equations of Plane Stress Transformation 644
- 14.3 Principal Stresses and Maximum In-Plane Shear Stress 647
- 14.4 Mohr's Circle—Plane Stress 659
- 14.5 Absolute Maximum Shear Stress 670
- 14.6 Plane Strain 675
- **14.7** General Equations of Plane-Strain Transformation 676
- 14.8 Mohr's Circle—Plane Strain 684
- \*14.9 Absolute Maximum Shear Strain 691
- 14.10 Strain Rosettes 693
- 14.11 Material Property Relationships 697



# 15 Design of Beams and Shafts 715

Chapter Objectives 715

- **15.1** Basis for Beam Design 715
- 15.2 Prismatic Beam Design 718



## 16 Deflection of Beams and Shafts 733

- 16.1 The Elastic Curve 733
- **16.2** Slope and Displacement by Integration 737
- \* 16.3 Discontinuity Functions 753
  - 16.4 Method of Superposition 764
  - **16.5** Statically Indeterminate Beams and Shafts—Method of Superposition 772



# 17 Buckling of Columns 789

Chapter Objectives 789

- 17.1 Critical Load 789
- **17.2** Ideal Column with Pin Supports 792
- **17.3** Columns Having Various Types of Supports 798
- \*17.4 The Secant Formula 808

#### **Appendices**

- A. Mathematical Review and Expressions 820
- B. Geometric Properties of an Area and Volume 824
- C. Geometric Properties of Structural Shapes 826
- D. Slopes and Deflections of Beams 828

Fundamental Problem Solutions 830

Answers to Selected Problems 865

Index 879